



Roll No.

Total No. of Pages : 02

Total No. of Questions : 18

B.Tech. (Electrical Engg./ECE) (Sem.-2)

**MATHEMATICS-II**

Subject Code : BTAM-202-18 M.Code :  
76255

Time : 3 Hrs.

Max. Marks : 60

**INSTRUCTIONS TO CANDIDATES :**

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION - B & C have FOUR questions each.
3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
4. Select atleast TWO questions from SECTION - B & C.

**SECTION-A**

**Answer briefly :**

- 1) Is the differential equation  $3x y^2 \frac{dy}{dx} - x^{y+2} = 0$  exact?
- 2) Find the general solution of the Clairaut's equation  $y = px + p^3$ .
- 3) Find the Wronskian of the equation  $(D^2 + 1)y = \operatorname{cosec} x$ .
- 4) Solve the first order non-linear PDE  $p^3 - q^3 = 0$ .
- 5) Give the classification criteria of 2<sup>nd</sup> order partial differential equation.
- 6) Define the order of convergence of iterative methods.
- 7) Write Gauss forward formula for central difference interpolation.
- 8) Write Simpson's  $\frac{1}{3}$  rule of numerical integration.
- 9) Define the operators  $\Delta$  and  $\nabla$ .
- 10) Using Euler's method, evaluate  $y(0.1)$  correct to 3 decimals,  $y' - y^2 = 0$ ,  $y(0) = 1$ .

## SECTION-B

- 11) Solve the differential equation  $\frac{dy}{dx} = 2x^4y - 4x$ .
- 12) Solve the differential equation  $(D^2 + 2D + 1)y = 2e^{3x}$ .
- 13) Solve the 3<sup>rd</sup> order using separation of variables with  $u(x, 0) = 4e^{-x}$ .
- 14) Find  $f(0.07)$ , using Newton's forward difference formula, given that  $f(0.05) = 0.0500$ ,  $f(0.10) = 0.0999$ ,  $f(0.15) = 0.1987$ ,  $f(0.20) = 0.2571$ .

## SECTION-C

- $t, u(1) = 2$ . Estimate  $u(1.2)$  using Runge Kutta 15) Given the initial value problem  $\frac{du}{dt} = e^{-t}$  method of 4<sup>th</sup> order upto 3 decimals. (Take  $h = 0.1$ ).
- 16) a) Solve the Cauchy-Euler equation  $x^2 \frac{d^2y}{dx^2} + 3x \frac{dy}{dx} + 3y = 0$  with  $y(1) = 0$ ,  $y'(1) = -2$ .
- b) Solve the partial differential equation  $\frac{\partial z}{\partial x^2} + \frac{\partial z}{\partial y^2} = x^2y$ .
- 17) a) Find  $\sqrt[3]{25}$  using Newton Raphson method.

1

- b) Evaluate  $\int_0^1 x^2 dx$ , using Trapezoidal rule by taking 7 subintervals.

$1 \int_0^x$

0

- 18) a) Using Taylor's series, find value of  $y$  at  $x = 0.1$  upto 3 decimals from

$$\frac{dy}{dx} \Big|_{x=1}, (0) \quad y(0)$$
$$\frac{d^2y}{dx^2} \Big|_{x=1}$$

- b) Using finite difference method, solve  $y'' + y + 1 = 0$ ,  $y(0) = y(1) = 0$  (Take  $h = 1/3$ ).

**NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.**